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Abstract	Edge detection plays an important role in many computer vision systems. In this paper, we propose a novel application agnostic algorithm for prediction of probabilities based on the contextual information available and then apply the algorithm for estimating the probability of pixels belonging to an edge using surrounding pixel values as local contexts. We then proceed to test different image transformations as input layers, such as the Canny edge detector. We propose two different architectures, one single layered and one multilayered, which approach the scaling problem by creating scaled side outputs and combining them via a logistic regression layer. We tested our approach on the BSDS500 edge detection dataset with optimistic results.	
Keywords (separated by '-')	Edge detection - Local context - Neural network - Probabilistic method - BSDS500 benchmark	



2 A novel contextual memory algorithm for edge detection

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6 Abstract

7 Edge detection plays an important role in many computer vision systems. In this paper, we propose a novel application agnos-
8 tic algorithm for prediction of probabilities based on the contextual information available and then apply the algorithm for
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10 test different image transformations as input layers, such as the Canny edge detector. We propose two different architectures,
11 one single layered and one multilayered, which approach the scaling problem by creating scaled side outputs and combining
12 them via a logistic regression layer. We tested our approach on the BSDS500 edge detection dataset with optimistic results.

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14 1 Introduction

15 The process of segmentation selects a set of pixels from
16 an image, based on rules and patterns. The labeling of the
17 extracted sets allows the user to obtain more information
18 from the image. Typical rules for segmentation include the
19 grouping of pixels by color, intensity or texture. Neverthe-
20 less, by targeting information extraction, rules can head
21 toward finding edges of objects, areas, specific shapes and
22 volumes, when applied to stacks of images. Automatic anno-
23 tation of images and video gains more support each year.

24 Practical applications of image segmentation include
25 machine vision, control systems, object detection (for exam-
26 ple, face detection and pedestrian detection), recognition
27 tasks (for example, fingerprint and iris recognition) and last
28 but not least, medical imaging. Medical image segmenta-
29 tion borrows from many general-purpose segmentation tech-
30 niques but combines them with domain-specific knowledge
31 in order to obtain better results. Shape analysis and volume
32 evolution make medical image segmentation important for
33 diagnostics and treatment plans.

34 Recent methods, like deep learning through convolu-
35 tional neural networks (CNN), proved to give state-of-the-art
36 results in 2D benchmarks, but neural network architectures

for 3D image processing are only now starting to emerge. 37
Medical image segmentation integrated these techniques for 38
both 2D [1] and 3D [2] segmentations. 39

In this paper, we introduce a general algorithm for auto- 40
mated learning, which stands as a basis for various appli- 41
cations. We provide a description of the algorithm and 42
point out differences from various implementations tested. 43
To prove the effectiveness, we have applied and tested the 44
algorithm on an edge detection benchmark, with promising 45
results. As for now, the algorithm was applied only for 2D 46
images, but in the future, we plan to extend it for volumetric 47
images, as an application in medical imaging. 48

2 Related work 49

Edge detection has been a subject of research for many years, 50
with papers as early as 1975 [3]. Since then, a large num- 51
ber of techniques have been approached, targeting different 52
aspects of edge detection, like closed contours, human-like 53
perception or fast detection. In the following, we provide 54
an overview of more recent methods used, organized by the 55
main strategy of the algorithm. 56

In [4], a method based on oriented gradient signals is 57
described. These are obtained from splitting the input image 58
into the three CIELAB color channels and a texture channel. 59
After applying filtering on the channels with 17 Gaussian 60
kernels, the results are clustered using a K-means algorithm. 61
An image is formed using the result for each pixel on which 62

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63 a non-maximal suppression is applied. So far, only local
64 information was used for each pixel. For the global informa-
65 tion, spectral clustering is used. The probability of a pixel
66 belonging to the contour is a weighted combination of the
67 local and global information.

68 Real-time frame rates have been recently achieved using
69 random decision for edge detection [5]. Local image patches
70 were used as a basis for learning structure labels. These are
71 then mapped into a discrete space using a decision tree
72 which splits the data based on a decision function. Learning
73 was done by independently training the trees in a recursive
74 manner using information gain criteria.

75 Deep learning architectures started to prove state-of-
76 the-art results at impressive processing speed of 0.4 s using
77 the holistically nested edge detection (HED) architecture
78 [6]. The networks map whole image to image predictions
79 which provide a significant advantage as a global informa-
80 tion method. A convolutional neural network with hierarchi-
81 cal representations provides the high-level features, visible
82 as side outputs of the network. Deep supervision is used
83 for training the layers, which are blended using a weighted
84 fusion layer to provide the final image.

85 Relaxed deep supervision (RDS), proposed in [7], also
86 relies on deep learning, but the main difference from HED
87 is that RDS accepts as input predictions from other edge
88 detectors such as Canny, called relaxed labels. HED itself
89 is used as a provider for relaxed labels. The network tries to
90 eliminate most of the false positives from all the intermedi-
91 ate layers.

92 The current state of the art is another recent deep learning
93 approach based on richer convolutional features [8]. Similar
94 to HED, it has a phase of producing side outputs, but in
95 this case, a VGG16 architecture was used. Instead of using
96 only the final convolutional layers for merging like previous
97 approaches did, this architecture encapsulates in a holistic
98 manner features from all convolutional layers and then trains
99 the network via backpropagation.

100 Though the research on deep network focuses only on
101 developing network architectures and not new techniques,
102 other approaches are continually tested in the literature with
103 promising improvements for low-level features, with the
104 main advantage being that you do not need a powerful video
105 card to run these algorithms thus can run on most equipment
106 and the results are good enough for further processing. One
107 such algorithm which improves the Canny edge detector is
108 described in [9]. After applying an improved anisotropic
109 diffusion filter, gradient templates are used for four direc-
110 tions. Then, an adaptive threshold is computed based on the
111 histogram of the image, making the output more resilient
112 to noise.

113 Another algorithm of this type revolves around hierar-
114 chical graph partitioning [10]. The algorithm employed
115 is called Divide and Link, and it is used for a hierarchical

network clustering. Unlike our proposed method, pixels are
here modeled as nodes in a graph and a dissimilarity order
between pixels determines the clusters in the graph. The
regions are then transformed into a boundary map with a
selection of the largest area of neighbor regions to provide
the border.

3 Basis for the contextual memory

Before detailing the proposed algorithm, we will present
some methods and techniques which stand as a basis for the
concept of contextual memory.

3.1 Logistic regression

For a regression model, where the dependant variable is a
categorical, the logistic regression can be used. In our case,
the outcome is binary, where an image pixel belongs to a
certain group or not. Binary logistic regression is useful for
estimating the probability of class membership. Useful for
making such predictions, a single-layer neural network has
the output probability:

$$P_r(Y_i = 1|X_i) = p_i = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x_{(1,i)} + \beta_2 x_{(2,i)} + \dots + \beta_k x_{(k,i)})}} \quad (1)$$

where p_i is the probability that the output Y_i belongs to the
class, defined as a sigmoid function of a linear combination
of the k explanatory variables X , and β_j for $j = 1, \dots, k$ are
the parameters to be estimated, usually called coefficients
or weights. The sigmoid function takes any input $x \in \mathcal{R}$ and
outputs a value between zero and one, making it interpre-
table as a probability. This function is also preferred because
it has a continuous derivative.

$$y = \frac{1}{1 + e^{-f(x)}}, \quad \frac{dy}{dx} = \frac{y(1-y)df}{dx} \quad (2)$$

The inverse of the logistic function, sometimes called the
stretch function, is defined as:

$$g(t) = \ln\left(\frac{t}{1-t}\right) \quad (3)$$

There are numerous numerical ways to estimate the
coefficients [11]; relevant here is the stochastic gradient
descent. Minimizing a function by following the gradient of
the cost is called gradient descent. If the loss is accounted
for the entire training set or a subset of the training set, the
method is called batch gradient descent. If the batch is the
size of one, we will have a stochastic gradient descent. For
each instance i of the training set, we will make a predic-
tion and then suffer a loss. If we apply the backpropagation

156 algorithm, the weights will be updated according to the fol-
 157 lowing rule:

158
$$\beta_j = \beta_j + \alpha x_j (y_i - p_i) p_i (1 - p_i) \tag{4}$$

159 where β_j is the weight for the j th input variable x_j , p_i is the
 160 output probability for the instance i , and y_i is the label of
 161 the instance (0 or 1). The learning rate α , usually chosen
 162 empirically, limits the amount of correction for each coef-
 163 ficient. This is the gradient descent in weight space which
 164 minimizes the root-mean-square error.

165 Instead, if we want to minimize the relative entropy
 166 $-\log(1 - p_i)$ if $y_i=1$ or $-\log(p_i)$ if $y_i=0$, then we will apply
 167 Eq. (5).

168
$$\beta_j = \beta_j + \alpha x_j (y_i - p_i) \tag{5}$$

169 This minimizes the amount of information lost when a
 170 prior probability distribution Q is used to approximate a
 171 posterior probability distribution P .

172 **3.2 Ensemble learning**

173 Combining multiple hypotheses in order to obtain a bet-
 174 ter hypothesis is called ensemble learning. Ensembles are
 175 supervised learning meta-algorithms which, after training,
 176 can be used to make predictions. The ensemble also repre-
 177 sents a hypothesis. The set of hypotheses which compose the
 178 ensemble do not necessarily contain the output hypothesis,
 179 making it likely to better describe the data. If not carefully
 180 prevented, this can lead to overfitting the training data.

181 As expected, using ensemble methods requires more
 182 resources (memory and computation time) than single mod-
 183 els. Various techniques make a trade-off between the speed
 184 of computation, amount of memory used and the accuracy
 185 of the model.

186 In the process of designing artificial neural networks, cre-
 187 ating multiple models and combining them are called ensem-
 188 ble averaging. The ensemble should perform better than the
 189 individual models because the error averages out. Instead of
 190 picking the prediction of only one of all the models as many
 191 ensemble techniques do, all the models are kept and the ones
 192 which are more prone to error are assigned a smaller weight.
 193 This can be expressed as a linear combination of experts.
 194 The output of the ensemble can be computed like in Eq. (6)

195
$$y(X; \alpha) = \sum_{j=1}^k \alpha_j y_j(x) \tag{6}$$

196 with α a set of weights, y_j as the j th model prediction.
 197 Numerically, optimizing α is already a solved problem when
 198 applying the neural network learning rules.

199 The properties of the models upon which the ensemble
 200 averaging is built upon are [12]:

1. In any network, the bias can be reduced at the cost of 201
 increased variance 202
2. In a group of networks, the variance can be reduced at 203
 no cost to bias 204

False assumptions in the learning algorithm lead to bias 205
 error. High bias leads to missing the correlations between 206
 the data features and the target outputs (under fitting). Sen- 207
 sitivity to small fluctuations in the training set causes vari- 208
 ance error. High variance can cause overfitting, meaning 209
 that the model has learned mostly noise instead of general- 210
 izing for unseen data. Given trained models with low bias 211
 but high variance, the result of the ensemble averaging is 212
 expected to have both low bias and low variance. 213

One of the variants of ensemble averaging is the nega- 214
 tive correlation learning. This algorithm attempts to train 215
 and to combine individual networks in an ensemble in the 216
 same learning process [13]. 217

Boosting is meta-algorithm which aims to create a 218
 strong learner from a collection of weak learners. As a 219
 rule of thumb, a series of weak classifiers are trained with 220
 respect to a probability distribution and are added to the 221
 set which is the basis for the strong classifier. This sequen- 222
 tial introduction of weak learners keeps them focused on 223
 the samples previous learners misclassified. 224

AdaBoost, short for “adaptive boosting”, is a type of 225
 ensemble learning. A boost classifier has the following 226
 form: 227

228
$$F_T(x) = \sum_{t=1}^T f_t(x) \text{ with } f_t(x) = \alpha_t h(x) \tag{7}$$

$f_t(x)$ is a weighted weak learner, while x is the sampled 229
 input. For a binary classification task, the output of the 230
 learner is considered of class 0, if the value is negative, or 231
 class 1, if the value is positive. The absolute value of the 232
 output should be interpreted as confidence in the result. 233

The output of a weak learner for the sample i is called 234
 the hypothesis $h(x_i)$. At iteration t , a weak learner is cho- 235
 sen and weighted with a coefficient α_t . The value of α_t 236
 should minimize E_t which is the training error at stage t . 237
 The error is computed using Eq. (8) 238

239
$$E_t = \sum_i E(F_{t-1}(x_i) + \alpha_t h(x_i)) \tag{8}$$

where $F_{t-1}(x)$ is the boosted classifier built up to the pre- 240
 vious stage and $E(F)$ is an arbitrarily chosen error func- 241
 tion. Recently, convex potential boosters received criticism 242
 regarding convergence where random classification noise is 243
 present [14]. 244

Stacking refers to blending the predictions of multi- 245
 ple machine learning models. With a specifically given 246

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247 combiner algorithm, stacking can represent most if not all
 248 ensemble techniques. Usually, a logistic regression layer
 249 is used as the combiner.

250 **3.3 Context modeling**

251 Context modeling describes how the context information
 252 is structured and maintained. Depending on the problem,
 253 different types of discriminator contexts are useful. Local
 254 context refers to the aspect of the data examined, as opposed
 255 to context value, which represents the numeric value of that
 256 context. The context value will be used for accessing the
 257 memory structure. The memory takes a context value as
 258 input and outputs a value used for computing the output
 259 probability of belonging to a certain class.

260 When discussing edge detection and describing whether
 261 a pixel belongs to an edge or not, one of the most important
 262 aspects to take into consideration is the neighboring pixels.
 263 For instance, as a context, we can take the top pixel and left
 264 pixel. The context value for this example would be top pixel
 265 intensity 255, left pixel intensity 20.

266 Choosing neighboring pixels means using a local context,
 267 because we do not input the entire image when deciding if
 268 the focused pixel is an edge or not. Even more, there is no
 269 clear rule on how far away we should look when making
 270 such an assumption.

271 We can define contexts as rays, starting from the focused
 272 pixel and going in a straight line away in a given direction.
 273 Rays are defined by direction and length. Rays could be chosen
 274 from 1 to L , the maximum context length. We define
 275 direction by the angle of the ray, and we choose the angle by
 276 dividing 360 degrees by the number of rays we want to use.
 277 For example, if we use 8 rays, we have 4 rays, one for each
 278 axis, and 4 rays for the diagonals, as in Fig. 1, for length 5
 279 and 8 rays.

280 The context value need not be only pixel values; we
 281 can take any function of the pixel values as well. Instead
 282 of directly using the values of the pixels, we can take the
 283 numerical derivative of the pixels in the direction of the
 284 ray. Of course, one can mask or quantize the values of the

pixels or the value of the derivative. In the case of color
 images, rays for each color channel can be individually taken
 as contexts.

288 **3.4 Resources and hashing as a solution**

289 If we allow contexts of any length to be used, we quickly hit
 290 the wall of practical limitations. Take, for instance, context
 291 values as pixels from a color channel which are represented
 292 as bytes. A context of length only 4 already means 2^{32} possible
 293 values. But not all the values will be relevant, as most
 294 of the possible values will represent noise.

295 To overcome this issue, we use hashing functions to
 296 map them to the chosen data structures. A hashing function
 297 maps data of arbitrary size to data of fixed size. This makes
 298 them useful for data structures like hash tables. One at a
 299 time hash functions are useful for data which comes in byte
 300 chunks, especially when we want to keep the intermediary
 301 hash values.

302 For the current work, we analyzed in particular two different
 303 types of hash functions: Jenkins hash function [15]
 304 and Fowler–Noll–Vo hash function [16]. Both of them are
 305 non-cryptographic but were chosen for their speed of computation
 306 and rather low collision rate.

307 Both functions can be altered to keep the intermediate
 308 results of the hash value, useful when working with rays of
 309 increasing length.

310 **4 An original method for contextual prediction**

311 Applied on images, the context modeling part of the algorithm
 312 takes as input an image and a position. The position
 313 is used as a basis for the rays which are modeled as position
 314 deltas from the focused pixel. The values of the pixels
 315 are taken from the color channel of the image and are then
 316 hashed. The result of the hash is the context value, which we
 317 later use for indexing. As a result, we have as many context
 318 values (numbers) as the number of contexts.
 319

320 The memory can be organized as a map with a separate
 321 table for each context in order to prevent collisions between
 322 contexts. There are more ways to organize the memory, and
 323 some suggestions will be discussed in the implementation
 324 details.

325 **4.1 Model prediction**

326 In order to make a prediction, we have proposed the following
 327 algorithm:

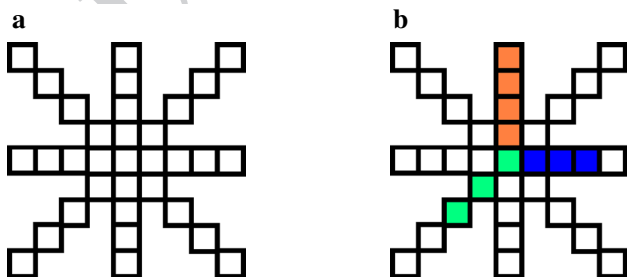


Fig. 1 a Position of pixels as rays of length 5; b ray length 3 (green), length 4 (blue) and length 5 (orange)

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- 328 1. We obtain a value from the memory for each context.
- 329 One way to do that is to index the hash of the context
- 330 value in a table
- 331 2. We average all the obtained memory values
- 332 3. Convert the average into a probability using the sigmoid
- 333 function
- 334 4. Refine the probability using a transfer function and
- 335 obtain the output probability (Eq. 9)

$$p = T\left(\sigma\left(\frac{k}{n} \sum_{i=0}^n v_i\right), C\right) \text{ with } v_i = M[i][hash(c_i)] \tag{9}$$

337 where p is the probability that the pixel belongs to a
 338 class (output probability), n is the number of input con-
 339 texts, c_i is the context value of the i th context, v_i is
 340 the value from the memory M for context i , k is some ad
 341 hoc constant, T is an adaptive probability map transfer
 342 function which takes as input a probability and a small
 343 context value C and outputs a refined probability, and σ
 344 is the sigmoid function.

345 The adaptive probability map (APM), sometimes called
 346 secondary symbol estimation (SSE), is used to fine tune a
 347 probability and works in the following way:

- 348 • Select a set of interpolation points according to a context
- 349 value C : $points = pointset[C]$
- 350 • Find the two points indexes between which the input
- 351 value falls: index low and index high
- 352 • Output the probability as the weighted average of the two
- 353 values from the points. The weight is selected from how
- 354 far the input is from the two points:

$$\begin{aligned} \text{Output} = & \text{points}[\text{index low}] * (1 - \text{weight}) \\ & + \text{points}[\text{index high}] * \text{weight} \end{aligned} \tag{10}$$

356 The input probability p can be mapped to point indexes in
 357 more ways. A simple way is to quantize the probability linearly
 358 to the number of points N_p . This is equivalent to

$$\text{Index low} = \lfloor p * N_p \rfloor, \quad \text{Index high} = \lfloor p * N_p \rfloor + 1 \tag{11}$$

where $\lfloor \cdot \rfloor$ denotes the floor operation.

Another way to quantize the probability is to stretch the
 probability first and then quantize linearly to the number of
 points. This serves the purpose to allocate more points close to
 zero and one, where fine-tuning makes more sense. The input
 value for the APM is now a stretched probability.

The following two diagrams plot the initial point values for
 the two methods described with respect to the input. When no
 value was changed, the output of the APM should be equal to
 the input probability. The X-axis represents the input value to
 be quantized, and the Y-axis represents the point values (prob-
 ability) (Fig. 2).

In logistic regression, every feature is individually weighted
 before applying the sigmoid function to the result. There is no
 assumption about the origin of the numeric value of the fea-
 ture. When we know that the input features are probabilities,
 logistic regression can be seen as a way of combining them.
 Mattern [17] proved that if instead of using plain probabilities
 as input, we use stretched probabilities (inverse logistic func-
 tion), that logistic mixing is optimal in the sense of minimizing
 Kullback–Leibler divergence, or wasted coding space, of the
 input predictions from the output mix. Stretching the input
 probabilities makes logistic regression a form of geometric
 weighting instead of linear weighting:

$$\beta_0 + \beta_1 x_{1,i} + \beta_2 x_{2,i} + \dots + \beta_k x_{k,i} \tag{12}$$

where $x_{j,i}$ is a probability becomes

$$\beta_0 + \beta_1 t_{1,i} + \beta_2 t_{2,i} + \dots + \beta_k t_{k,i} \tag{13}$$

where $t_{j,i} = \ln\left(\frac{x_{j,i}}{1-x_{j,i}}\right)$ and the update formula for minimizing
 the relative entropy could be written:

$$\beta_j = \beta_j + \alpha t_j (y_i - p_i) \tag{14}$$

Coming back to our case, we ask the question: where
 does the predictive power of an ensemble come from?
 Where does this information lay, in the aggregating

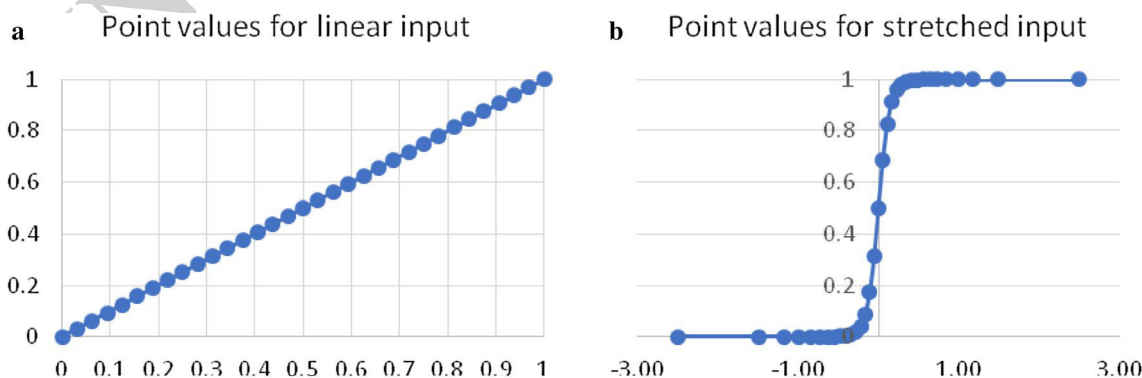


Fig. 2 a Uniform distribution of points; b non-uniform distribution of points

393 algorithm or the individual components? It is obvious that
 394 if we use a form of logistic regression, the set of weights
 395 carries some information. It can be argued if that more
 396 weights are somehow added to the aggregating algorithm,
 397 it would be beneficial to its predictive power.

398 To some extent following this, an algorithm that adds
 399 more layers of logistic regression is the context mixing
 400 algorithm. The algorithm has been successfully applied in
 401 state-of-the-art data compression programs like PAQ [18]
 402 and *cmix* [19], which rank first in most text and general
 403 data compression benchmarks for their compression ratio.

404 The algorithm works in the following way:

- 405 • Instead of mixing the input probabilities with only one
- 406 set of weights, create a number N of buckets of sets of
- 407 weights
- 408 • Choose one set of weights from each of the N buckets
- 409 according to a function of context
- 410 • Applying logistic regression with each set of weights
- 411 will result in N probabilities, which will be mixed by
- 412 another set of weights chosen from its own bucket.

413 One could underline that some information regarding
 414 context is passed to the mixing ensemble, hence the name
 415 context mixing. If instead we want to move the mixing
 416 information from the ensemble toward the weak learners,
 417 we need to take into consideration the following: How
 418 to pass information back to the learners? We made little
 419 assumptions so far about the value of v_i . We know that
 420 the value comes from a big bucket of entries, where its
 421 index is dependent on the context. In a regression sense,
 422 the feature is the context, not v_i . We interpret this value
 423 like $v_i = \beta_i + t_i$, where t_i is a stretched probability for the
 424 context value and β is the weight of the probability in the
 425 ensemble. Averaging the memory values:

$$426 \frac{k}{n} \sum_{i=0}^n \beta_i t_i \quad (15)$$

427 which itself is a stretched probability. Applying the sigmoid
 428 function converts this average back into a probability.

429 **4.2 The proposed model update**

430 To update the model, we propose dual objective
 431 minimization:

- 432 • Minimize the error with respect to the output of the entire
- 433 network
- 434 • Minimize the error with respect to the output of the indi-
- 435 vidual node

436 An important remark here is that we can update the model
 437 from a supervised learning point of view or from a rein-
 438 forcement learning point of view. Supervised learning means
 439 that we know the precise probability for the case we were
 440 predicting, and we use that for backpropagation. Reinforce-
 441 ment learning means we do not know the exact probability
 442 for the case and do not even know how to obtain it, but
 443 instead we rely on maximizing a cumulative reward in an
 444 on-line manner, given the interaction with the environment.
 445 In our case, instead of backpropagating a probability, we can
 446 use the binary outcome instead and try to minimize either
 447 the cumulative logistic loss or the cumulative square loss
 448 (Fig. 3).

449 Working with stretched probabilities for logistic regres-
 450 sion results in the global update error to be:

$$451 E_g = \beta_g(p - y) \quad (16)$$

452 for minimizing logistic loss, or

$$453 E_g = \beta_g(p - y)p(1 - p) \quad (17)$$

454 for minimizing the square loss, where E_g is the global error,
 455 β_g is the global error learning rate, p is the output probability
 456 and y is the information available as ground truth, that can
 457 be a binary outcome or a probability.

458 After computing the global error, we proceed in comput-
 459 ing local errors for each memory value and updating them.
 460 The local error is defined as:

$$461 E_l = \beta_l(p_i - y) \text{ with } p_i = \sigma(v_i) \quad (18)$$

462 for minimizing logistic loss, or

$$463 E_l = \beta_l(p_i - y)p_i(1 - p_i) \text{ with } p_i = \sigma(v_i) \quad (19)$$

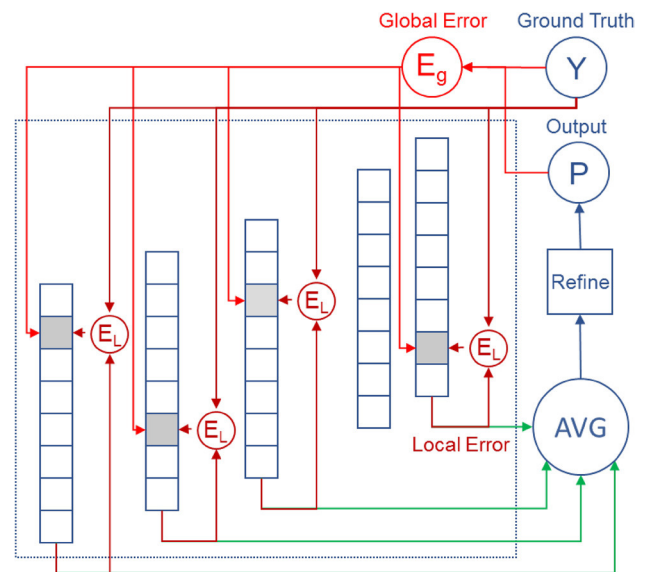


Fig. 3 Block scheme for the proposed update algorithm

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464 for minimizing the square loss, where E_l is the local error, β_l
 465 is the local error learning rate, p_i is the output probability for
 466 the i th context (side prediction), computed as the sigmoid of
 467 the memory value v_i , and y is the ground truth.

468 Each memory value is then updated by subtracting both
 469 the local and the global errors:

470
$$v_i = v_i - E_l - E_g \quad (20)$$

471 It is important to notice that the global error is computed
 472 using the output probability which was refined by the adap-
 473 tive probability map. This is not mandatory, but our tests
 474 show better results when the refined probability is used. This
 475 can be seen as allowing the model to learn something that
 476 can be corrected.

477 Updating the adaptive probability map works in the fol-
 478 lowing way: the point values for *index high* and *index low*
 479 are adjusted to reduce the prediction error. Error for index
 480 low is

481
$$(\text{Points}[\text{index low}] - y) * (1 - \text{weight}) * \text{learning rate} \quad (21)$$

482 the error for *index high* is

483
$$(\text{Points}[\text{index high}] - y) * \text{weight} * \text{learning rate} \quad (22)$$

484 where y is the ground truth available. Of course, variations
 485 of this can be applied, such as updating only the closest
 486 value.

487 Compared with the logistic regression, this method does
 488 not update the weights of the mixture, since the combining
 489 function is not a dot product, but it updates directly the val-
 490 ues which participate in the average.

491 It is still a form of ensemble learning, particularly ensem-
 492 ble averaging, where the elements of the ensemble here are
 493 the memory values. The ensemble error is the global error.

494 One can argue that this method is similar to boosting,
 495 regarding the fact that each side prediction is a weak learner,
 496 and the output after mixing is the strong learner. Depend-
 497 ing on the memory implementation chosen, which will be
 498 discussed in the next chapter, additional and possible longer
 499 contexts with unseen data make up for the bias of shorter
 500 contexts and can be added or evicted when accounting for
 501 the memory size limitations. Even though the error is back-
 502 propagated depending on the context, it also differs from
 503 context mixing, because there is no mixing layer to separate
 504 the context weights from the input probabilities.

505 **5 Results**

506 **5.1 Inputs, preprocessing and processing**
 507 **architecture**

508 We implemented the contextual memory algorithm for
 509 an edge detector application. This section describes the

architecture and some of the implementation details of 510
 the application. The application is implemented in the C# 511
 programming language, since we wanted to not restrict the 512
 testing and usage of the application to a closed scripting 513
 environment like MATLAB. Using a strongly typed pro- 514
 gramming language also helps with choosing better data 515
 structures. The source code is publicly available at the 516
 GitHub page [https://github.com/AlexDorobantiu/Conte](https://github.com/AlexDorobantiu/ContextualMemoryEdgeDetection)
 517 [xtualMemoryEdgeDetection](https://github.com/AlexDorobantiu/ContextualMemoryEdgeDetection). 518

519 Even when talking about two-dimensional images,
 520 color images have more layers in the dimension of the
 521 RGB colors. Hence, three layers can go as an input for the
 522 algorithm. These layers are preprocessed using a chain of
 523 preprocessors. We used a Gauss filter for eliminating the
 524 noise in the input images. This takes the original RGB
 525 layers as input and outputs a three-layer image. We used a
 526 filter of size 5 and a sigma value of 1.4.

527 Since the algorithm makes no assumption of the data
 528 behind contexts, it can be benefic to include transfor-
 529 mations of the color layers. Such transformations are
 530 appended as other layers for the algorithm input image. We
 531 optionally used the Sobel filter, the Canny edge detection
 532 algorithm and a Kirsch edge detection algorithm as input,
 533 which take the color channels and output another layer.
 534 This makes the final input image to have three or more lay-
 535 ers. Having a Canny layer, or any edge detector as input, is
 536 a sort of domain-specific knowledge added in the model.

537 The single-layer architecture takes a preprocessed
 538 image as an input and uses a given set of color channels to
 539 compute an output image which consists of a single-layer
 540 grayscale image in which the pixels represent the probab-
 541 ility that the position in the original image belongs to
 542 an edge. The single-layer architecture combined with the
 543 simple rays as contexts does not take into account infor-
 544 mation about the edge being kept the same at different
 545 zoom levels.

546 To tackle the zooming problem, the multilayer archi-
 547 tecture behaves in this way: take the original image, apply
 548 preprocessing, obtain the output; then take the original
 549 image, apply the preprocessing, append the previously
 550 obtained output as a layer, resize the image (meaning all
 551 its layers), and use it as an input for the algorithm. If one
 552 decides to separate the memory used by the algorithm at
 553 different sizes, we have a multilayer architecture. Each
 554 layer is trained separately starting from the largest image
 555 and going toward resized images. An algorithm layer can
 556 have different configurations from the other layers, and
 557 options can include the length of the longest ray, the pre-
 558 processing done, the memory size and others. The result
 559 of the multilayer architecture is a set of grayscale images
 560 of varying sizes, which are called side outputs. These
 561 side outputs are then combined (blended) using a logistic
 562 regression layer, to form a single image. Before blending,

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563 the images are scaled to have the same size. The weights
 564 of the logistic regression layer are also trained on the training
 565 set.

566 **5.2 Results on Berkeley edge detection benchmark**

567 In this chapter, we present one example of the output images
 568 from the algorithm using image “326025.jpg” from the men-
 569 tioned benchmark dataset along with some of the parameters
 570 used and a short description of the differences. We also pro-
 571 vide an analytical evaluation of the improvements compared
 AQ1 AQ2 to the Canny edge detection method (Fig. 4).

573 The global parameter values used in the tests were
 574 $\beta_l=0.25$, $\beta_g=0.5$ and $k=2$, and quantized derivative rays
 575 have the two least significant bits quantized. The results for
 576 single-layer architecture are shown in Table 1, (Table 2 and
 577 Fig. 5).

578 Before computing the score for the benchmark, the output
 579 images are subjected to a non-maximal suppression techni-
 580 que and subsequently to an edge thinning. This is done in
 581 MATLAB, using an adapted version of the Piotr Dollar’s
 582 Structured Edge Detection Toolbox, available at [https://github](https://github.com/pdollar/edges)
 583 [b.com/pdollar/edges](https://github.com/pdollar/edges).

584 The benchmark provides a tool for evaluation which
 585 has an automated search in the space of thresholding, so
 586 that the user feels free to leave grayscale images instead
 587 of making the binarization himself. We compare the algo-
 588 rithm with the well-known Canny edge detector, the recent
 589 ID&L algorithm [10] and to the state-of-the-art deep learn-
 590 ing algorithms HED [6], RDS [7], RCF-ResNet101-MS
 591 [8], CED-VGG16 [20], AMH-ResNet50 [21], CASENet
 AQ3 [22] and CEDN [23] (Table 3).

593 We can clearly see from Fig. 6 that the learning is
 594 shifted toward not taking any risks, since the better F1
 595 score is achieved in the low threshold settings. In order to
 596 obtain an overall better F1 score, class balancing must be
 597 considered when applying the loss function.

598 We made another analytical comparison using the cross-
 599 entropy measure. If we have two probability distributions,
 600 we can measure the number of bits needed to identify an
 601 event drawn from a set if a coding scheme is used using a
 602 probability distribution other than the true distribution of
 603 the set. Since the pixel intensities in the resulting images
 604 can be modeled as a probability of a pixel belonging to
 605 an edge, we can measure the cross-entropy for the output
 606 images. We show a comparison with the Canny algorithm
 607 for the first 50 images in the test set of the benchmark in
 608 Fig. 7. A better probability modeling of the true source
 609 of the edges should have a lower cross-entropy. For the
 610 overall set, the proposed method obtained a cross-entropy
 611 of 6610784. In comparison, the Canny algorithm obtained
 612 a score of 11372700. This means that our algorithm sur-
 613 passed the Canny algorithm by a factor of 1.72.

614 To prove the potential of the proposed method, we also
 615 considered the precision with respect to the threshold.
 616 Precision is the fraction of relevant instances among the
 617 retrieved instances. A high value represents a small rate
 618 of false positives. Compared with the Canny algorithm,
 619 the proposed method offers a steady increase in precision
 620 and a roughly constant better precision with respect to the
 621 threshold. This can be seen in Fig. 8.

622 Provided the results on the three measures, we show
 623 that the proposed algorithm has potential over the Canny
 624 method.

625 **6 Conclusions**

626 The main contribution of this paper is an application
 627 agnostic algorithm for prediction of probabilities based
 628 on the contextual information available, where learning
 629 can be done in an on-line fashion. More than this, it does
 630 not impose any constraints on how to choose or model the
 631 context. This freedom allows it to be used in many areas

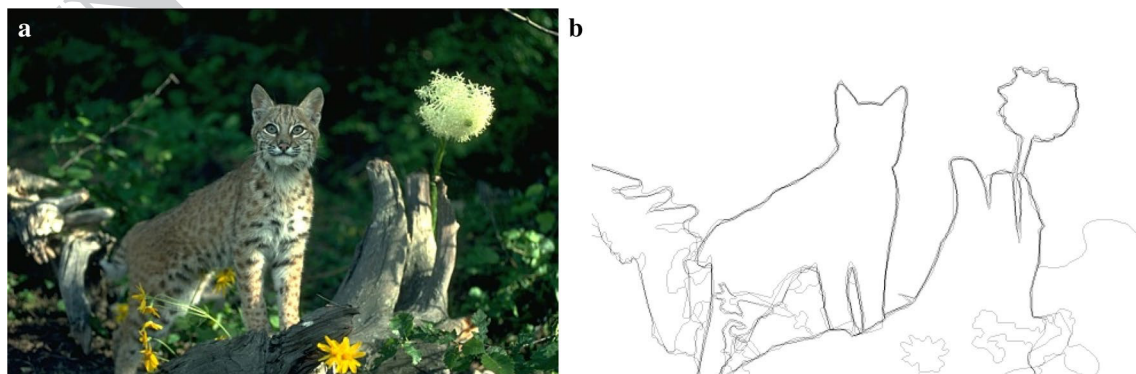






Fig. 4 a Sample image from the benchmark along with b the ground truth

Table 1 Some of the results for single layer


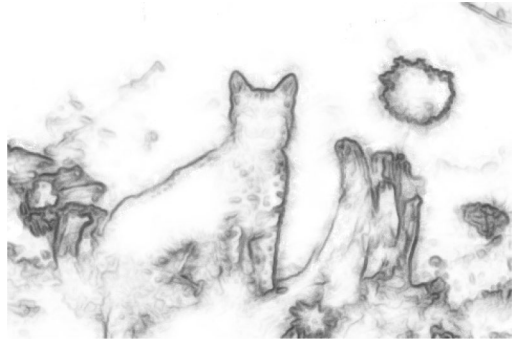
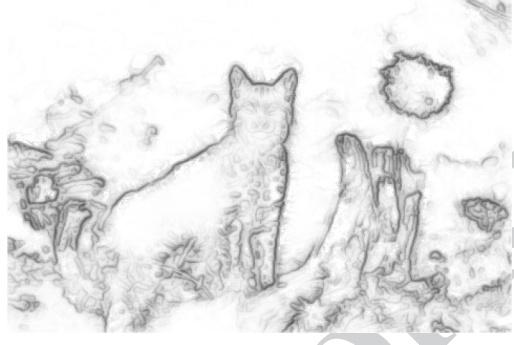
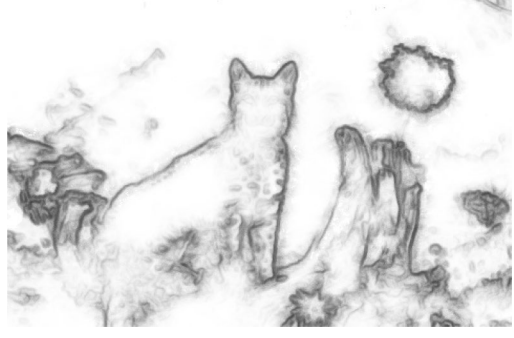
Algorithm output	Description
	Context model: 16 rays, max length: 8, including quantized derivative rays Memory: direct lookup, table size 218 Loss function: square loss Number of passes over training set: 1 Preprocess: Gauss
	Context model: 16 rays, max length: 8, including quantized derivative rays Memory: tagged lookup, table size 220 Loss function: square loss Number of passes over training set: 1 Preprocess: Gauss
	Context model: 16 rays, max length: 8, including quantized derivative rays Memory: bucket lookup, table size 220 Loss function: square loss Number of passes over training set: 1 Preprocess: Gauss, Canny, Kirsch
	Context model: 16 rays, max length: 8, including quantized derivative rays Memory: direct lookup, table size 220 Loss function: entropy loss, GT threshold: 63 Number of passes over training set: 1 Preprocess: Gauss, Canny, Kirsch

632 such as one-dimensional data, such as text information
 633 or data sequences, two-dimensional data, such as images,
 634 and three-dimensional data, such as volumetric images (or
 635 image slices which represent volumetric information). It

also allows it to be part of larger learning and prediction
 structures, having loose requirements on what information
 is needed for feedback.

636
 637
 638

Table 2 Some of the results for multilayer architecture

Algorithm output	Description
	<p>Context model: 16 rays, max length: 8, including quantized derivative rays Memory: direct lookup, table size 218 Loss function: square loss, GT threshold: 63 Number of passes over training set: 1 Preprocess: Gauss, Canny, Kirsch Layers scale: 1, 2, 4, 8, 16</p>
	<p>Context model: 16 rays, max length: 8, including quantized derivative rays Memory: bucket lookup, table size 219 Loss function: entropy loss, GT threshold: 63 Number of passes over training set: 1 Preprocess: Gauss Layers scale: 1, 3, 5, 7</p>
	<p>Context model: 16 rays, max length: 8, including quantized derivative rays Memory: bucket lookup, table size 219 Loss function: entropy loss, GT threshold: 63 Number of passes over training set: 1 Preprocess: Gauss, Canny Layers scale: 1, 3, 5, 7</p>
	<p>Context model: 16 rays, max length: 8 Memory: bucket lookup, table size 219 Loss function: entropy loss, GT threshold: 63 Number of passes over training set: 1 Preprocess: Gauss, Canny, Kirsch Layers scale: 1, 3, 5, 7</p>

639 In order to demonstrate the usefulness of the method,
 640 a 2D edge detection application using the method was
 641 implemented. The results are promising, considering that
 642 no prior handcrafted knowledge has been added in the
 643 model to help with the prediction.

644 Allocating too much memory and more training passes
 645 over the training set leads to overfitting. The algorithm
 646 will learn by heart the training set and will reproduce
 647 meticulously the ground truth, but the quality of the results

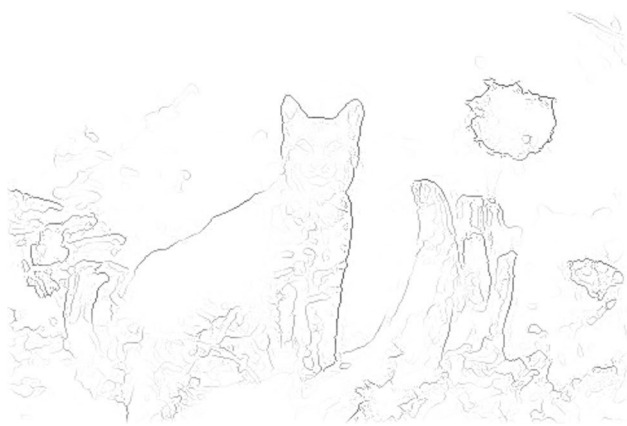


Fig. 5 Output example after NMS and thinning

Table 3 Comparative results

Algorithm	F1 score	Precision	Recall	Threshold
Canny	0.583	0.500	0.698	0.33
ID&L [10]	0.610	0.590	0.680	N/A
Contextual memory (proposed)	0.640	0.605	0.686	0.19
CASENet [22]	0.767	N/A	N/A	N/A
HED [6]	0.787	0.803	0.772	0.46
RDS [7]	0.792	N/A	N/A	N/A
CED-VGG16 [20]	0.794	N/A	N/A	N/A
AMH-ResNet50 [21]	0.798	N/A	N/A	N/A
CEDN [23]	0.788	N/A	N/A	N/A
RCF-ResNet101-MS [8]	0.819	N/A	N/A	N/A

648 on the test set will downgrade. We do not propose any
649 solution to the overfitting problem in this paper.

650 In the future, we intend to develop more in the direction
651 of contextual modeling, which means exploring the space
652 of choosing the appropriate contexts for various applica-
653 tions. We would also like to extend the existing applica-
654 tion for three-dimensional images and apply it for medi-
655 cal image segmentation. Some of the changes needed to
656 make when switching from 2D to 3D will be to model 3D

657 contexts, which can be chosen as rays in three dimensions
658 instead of two. Also, centerline and segmentation bench-
659 marks have different intended objectives, so the feedback
660 mechanism and the output metrics will have to be adapted
661 to obtain results relevant to those benchmarks.

662 In order to improve the existing application, the follow-
663 ing can be implemented:

- 664 • Replace the loss function with a cost-sensitive loss
665 function, as described in [13], because the distribution
666 of edge/non-edge pixels in the benchmark is biased
667 90% in favor of non-edges
- 668 • Model rays as individual blocks, whose output will be
669 combined using a context mixing layer. This means each
670 ray will output a probability, and the set of probabilities
671 will be further combined into a single probability
- 672 • Replace the blending algorithm with an improved context
673 mixing layer, maybe even with a fully connected layer
674 such as in CNNs
- 675 • Add more convolutional layers as input, having a set of
676 learnable filters
- 677 • Add the output of the state-of-the-art edge detectors as
678 input layers, to see how the algorithm balances the preci-
679 sion and recall
- 680 • Implement a GPGPU version of both the single and mul-
681 tilayer algorithm
- 682 • Adapt the training phase to iterate over transformed ver-
683 sions of the input images, such as rotations and scaling,
684 to gain more training data
- 685 • Exclude unconvincing ground truth data, when less than
686 a half of the human subjects agree to the edge position
- 687 • Last but not least, design space exploration with respect
688 to the parameters

689 Integrating with the relaxed deep supervision [7] algo-
690 rithm should provide interesting results, since algorithm
691 provides high precision on lower thresholds. We also expect
692 the proposed network to integrate well with a deep learning
693 architecture, especially with a CNN network, as a layer after
694 the rectified linear units (ReLU) layer, side by side with the
695 fully connected layer.

Fig. 6 F1 score plotted against threshold

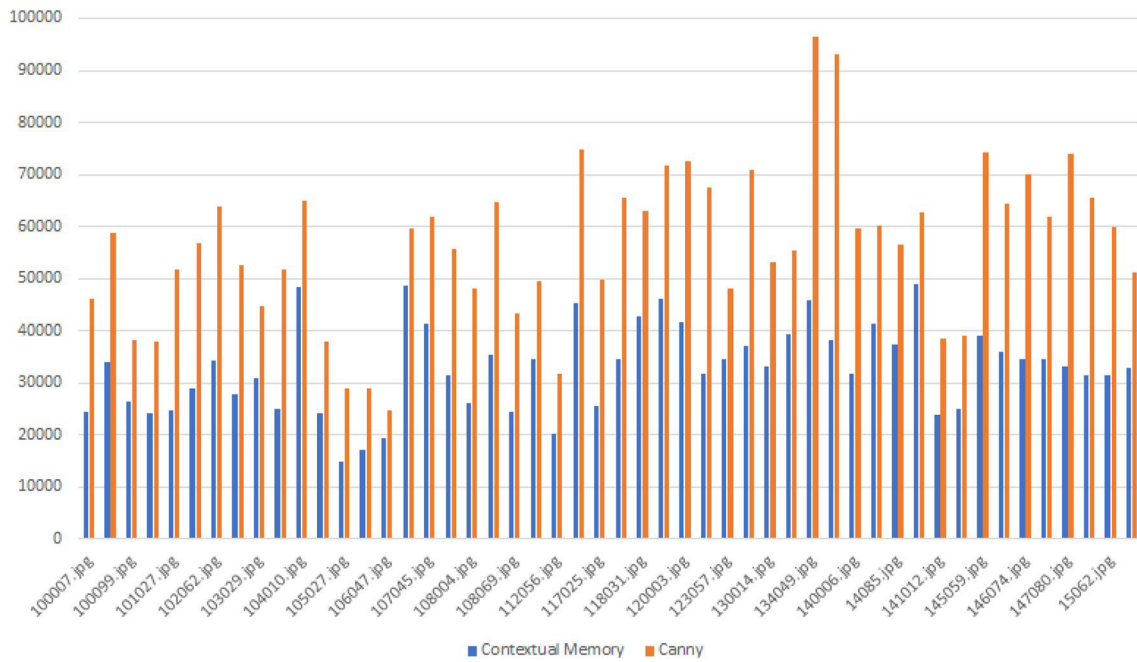
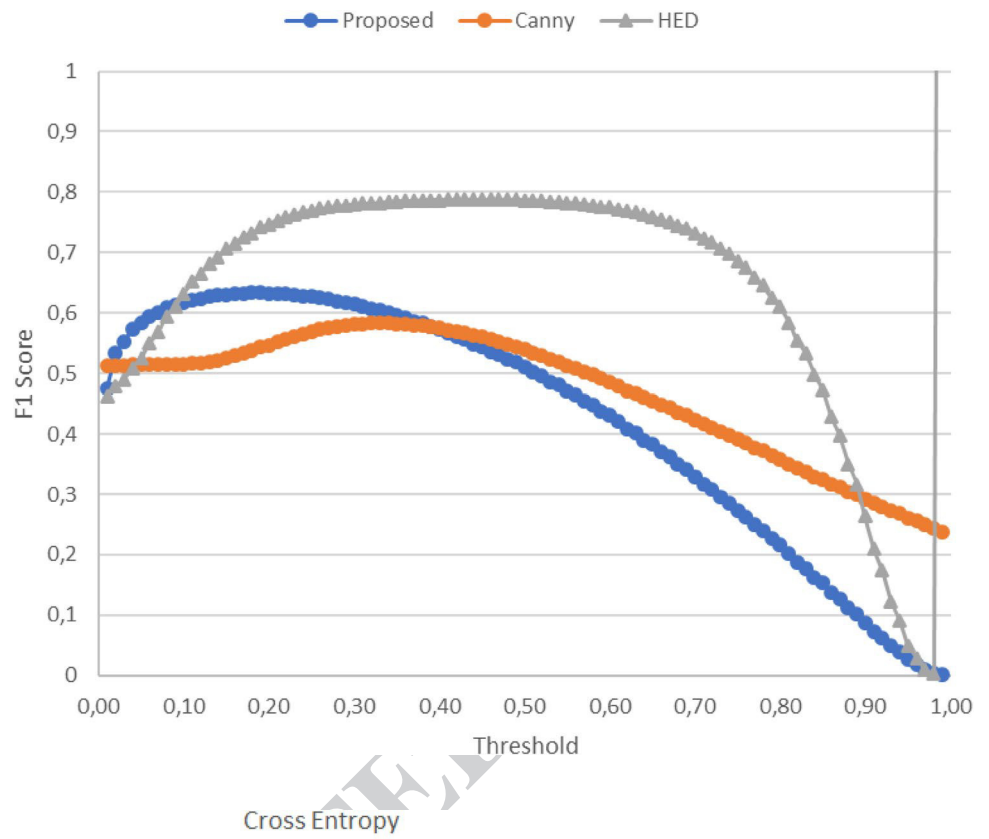
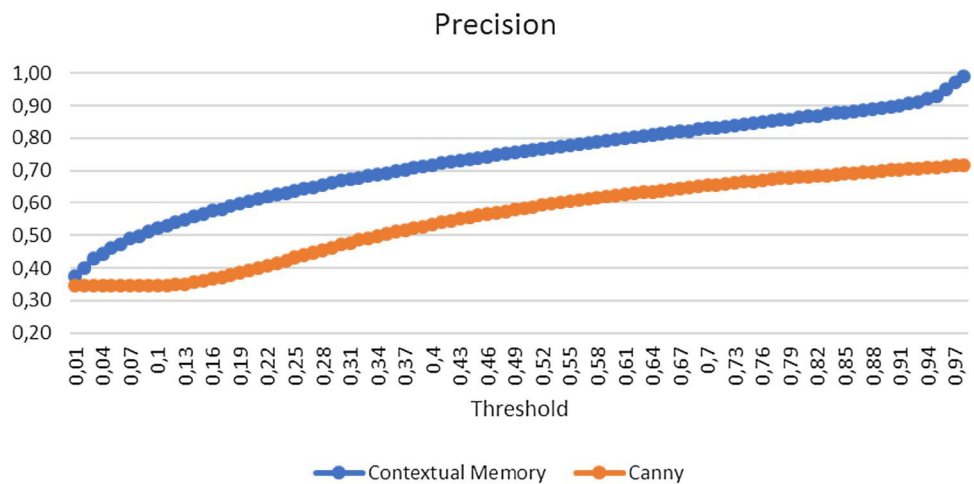


Fig. 7 Cross-entropy for the first 50 images of the dataset (lower is better)

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Fig. 8 Precision with respect to the threshold (bigger is better)



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